

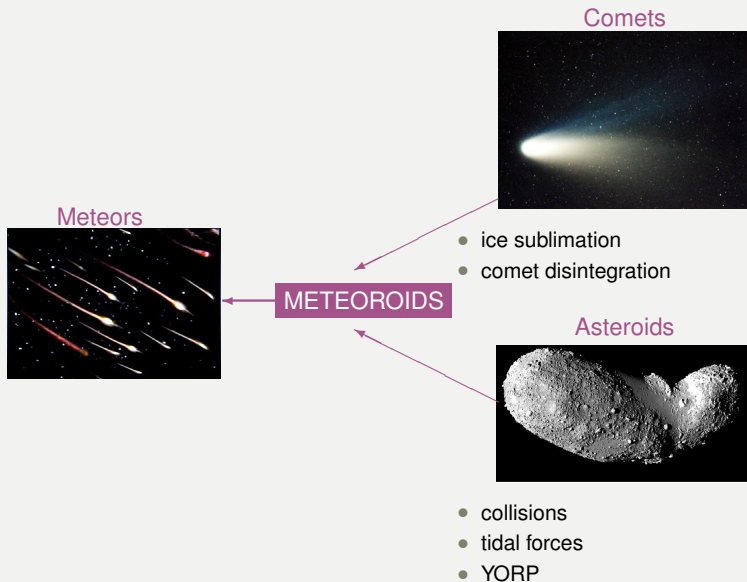


## The parent body search

**R. Rudawska, P. Atreya, S. Bouley,  
J. Vaubailon, F. Colas, T. Silbermann**

September 15-18, 2011





## Meteoroid stream identification methods

## How the search procedure looks like?

- Choose a meteoroid streams search algorithm:
  - iterative methods,
  - method of indices,
  - single linking method,
  - wavelet transform technique.
- Choose a dynamical similarity function - D-criterion.
- Choose a similarity threshold  $D_C$ .



## Dynamical similarity functions

- D-criterion based on the orbital parameters ( $q$ ,  $e$ ,  $i$ ,  $\Omega$ ,  $\omega$ ).

$$D_{SH}^2 = [e_B - e_A]^2 + [q_B - q_A]^2 + \left[ 2 \cdot \sin \frac{l_{BA}}{2} \right]^2 + \left[ \frac{e_B + e_A}{2} \right]^2 \left[ 2 \cdot \sin \frac{\pi_{BA}}{2} \right]^2$$

where

$e_A$ ,  $e_B$  – eccentricities of orbits A and B,

$q_A$ ,  $q_B$  – perihelion distances of orbits A and B,

$l_{BA}$  – the angle between the orbital planes,

$\pi_{BA}$  – the difference between the longitude of perihelion, measured from the intersection point of the orbital planes.

$l_{BA}$  and  $\pi_{BA}$  are expressed in terms of angular orbital elements (inclination  $i$ , longitude of the ascending node  $\Omega$  and argument of periapsis  $\omega$ ).

Southworth, R. B., Hawkins, G. S. 1963, *Smithson. Contr. Astrophys.*, 7, 261

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Joepke, T. J., 1993, Icarus, 106, 603

## Dynamical similarity functions

- D-criterion based on dynamical quasi-invariants.

$$D_V^2 = w_{h1}(h_{B1} - h_{A1})^2 + w_{h2}(h_{B2} - h_{A2})^2 + 1.5 w_{h3}(h_{B3} - h_{A3})^2 \\ + w_{e1}(e_{B1} - e_{A1})^2 + w_{e2}(e_{B2} - e_{A2})^2 + w_{e3}(e_{B3} - e_{A3})^2 \\ + 2 w_E(E_B + E_A)^2$$

where

$\mathbf{h}$  – the angular momentum vector,

$\mathbf{e}$  – the Laplace vector,

$E$  – the energy constant,

$w_h, w_e, w_E$  – the weighting factors.

Jopek, T. J., Rudawska, R., Bartczak, P. J. 2008, EM&P, 102, 73

## Meteoroid stream identification methods

## Dynamical similarity functions

- D-criterion based on dynamical quasi-invariants.

$$D_J^2 = \left( \frac{C_{A1} - C_{B1}}{0.13} \right)^2 + \left( \frac{C_{A2} - C_{B2}}{0.06} \right)^2 + \left( \frac{C_{A3} - C_{B3}}{14.^\circ 2} \right)^2$$

where

$C_1$  – corresponds to the z-component of the orbital angular momentum,

$C_2$  – is taken from the secular model of Lidov,

$C_3$  – invariant is the longitude of perihelion.

Jenniskens, P., 2008, Icarus, 194, 13

# The streams and their parent bodies

## Our parent body search procedure





# The streams and their parent bodies

## Meteoroid orbits sample

The model of generation and evolution of meteoroid stream in the solar system is taken from Vaubaillon *et al.* (2005)

- the nucleus is a mixture of water ice and dust,
- the nucleus is spherical and homogeneous,
- the water is produced in the sunlit hemisphere of the nucleus,
- the dust particles are spherical, homogeneous,
- the particles are ejected within 3.0 AU, from the Sun, in the sunlit hemisphere,

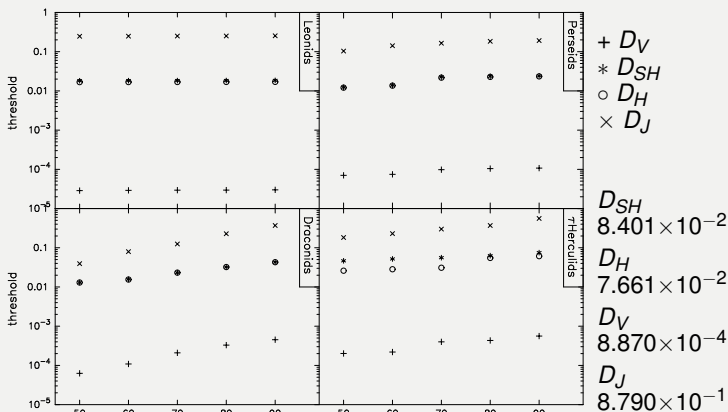


- the particles are submitted to the gravitational force of the Sun, the nine planets and the Moon, as well as to non-gravitational forces.

Vaubaillon, J., Colas, F. & Jorda, L., *Astronomy and Astrophysics*, Vol. 439, p. 751, 2005

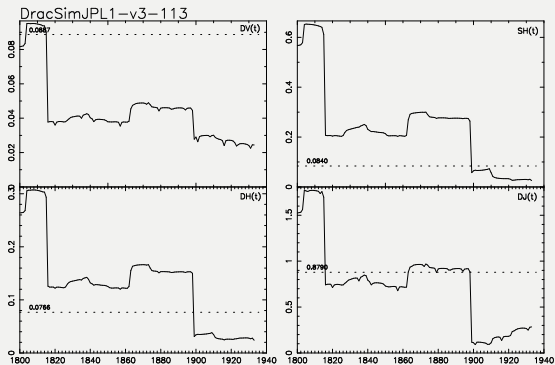
## Results

## Determining the threshold from experimental data



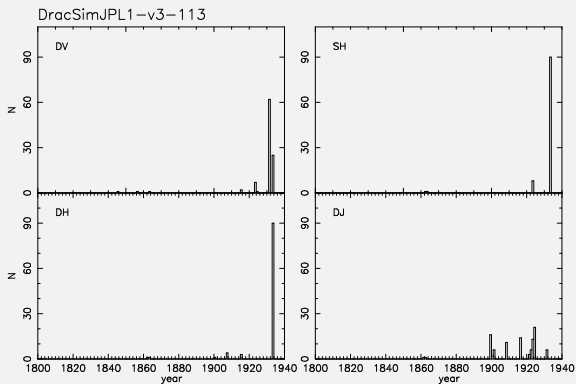
## Results

## Looking for the epoch of ejection



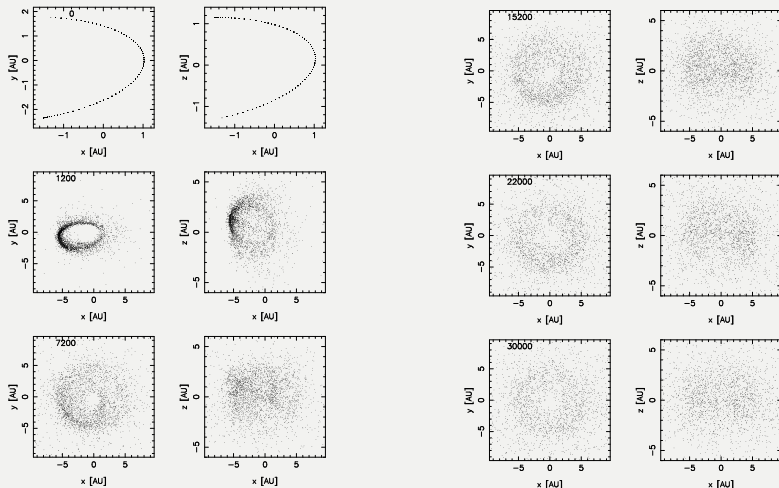
## Results

## Looking for the epoch of ejection



## The streams and their parent bodies

## Orbital evolution of the Draconids stream



Rudawska, R., 2010, In Ph.D. dissertation, A. M. University, Poznan

# Results

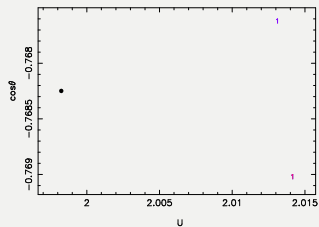
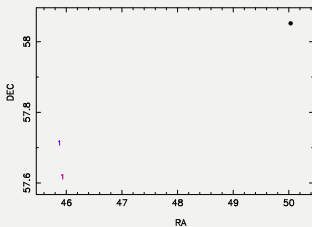
## Application

- The obtained values of thresholds were applied to a sample of the Armagh Observatory meteor data.
- Atreya, P., 2009, In Ph.D. dissertation, Armagh Observatory, Armagh, Northern Ireland.
- Double station meteors: 457 meteor orbits.

## Results

## Application

2005AUG14; JD: 2453596.526030

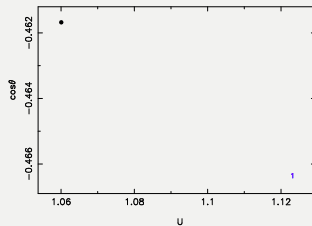
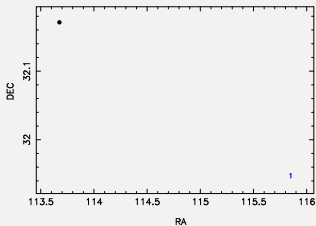


	RA	DEC	Vgeo	U	cos $\theta$	d_RaDec	d_Ucos $\theta$	
	50.0328	58.0521	59.0382	1.9982	-0.7682			: meteor
1	45.9321	57.6114	59.4196	2.0141	-0.7690	4.1243	0.0159	: 109P/Swift-Tuttle
1	45.8760	57.7067	59.4074	2.0131	-0.7676	4.1711	0.0149	: 109P/Swift-Tuttle
1	45.9321	57.6114	59.4196	2.0141	-0.7690	4.1243	0.0159	: 109P/Swift-Tuttle

## Results

## Application

2007DEC14; JD: 2454448.709213



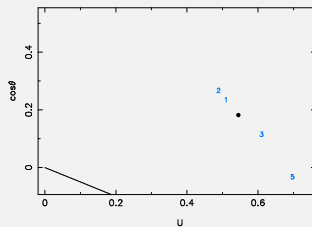
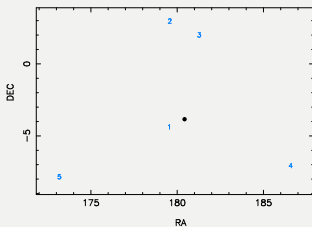
	RA	DEC	Vgeo	U	$\cos\theta$	d_RaDec	d_Ucos $\theta$	
	113.6751	32.1712	31.7751	1.0601	-0.4617			: meteor
1	115.8492	31.9443	34.0965	1.1231	-0.4664	2.1859	0.0633	: Phoethon
1	115.8492	31.9443	34.0965	1.1231	-0.4664	2.1859	0.0633	: Phoethon



## Results

## Application

2006APR02; JD: 2453827.549039

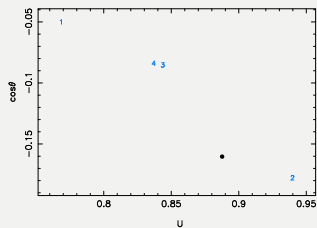
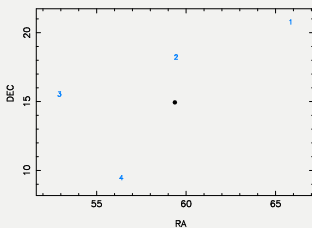


	RA	DEC	Vgeo	U	cos $\theta$	d_RaDec	d_Ucos $\theta$	
	180.4290	-3.8414	16.7103	0.5448	0.1819			: meteor
1	179.5448	-4.5413	18.4479	0.5101	0.2269	1.1277	0.0569	: 2003 BD44
2	179.5763	2.8180	14.1462	0.4890	0.2594	6.7137	0.0955	: 2009 FP32
3	181.2776	1.8558	14.8791	0.6100	0.1075	5.7600	0.0990	: 2006 BC10
4	186.5776	-7.2185	7.3052	0.0461	5.6353	7.0150	5.4762	: 2002 JQ97
5	173.1768	-7.9903	21.2457	0.6972	-0.0396	8.3552	0.2688	: 2004 ST26

## Results

## Application

2005NOV12; JD: 2453687.490926

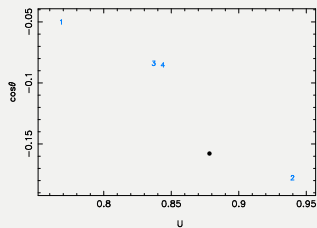
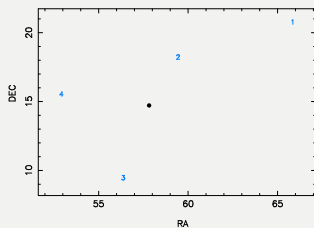


	RA	DEC	Vgeo	U	cos $\beta$	d_RaDec	d_Ucos $\beta$	
	59.3718	14.9404	26.2150	0.8877	-0.1603			: meteor
1	65.8418	20.6078	14.4153	0.7685	-0.0520	8.6011	0.1611	: 2005 UW6
2	59.4412	18.0680	24.7943	0.9398	-0.1795	3.1283	0.0555	: 2010 TU149
3	52.9191	15.3793	26.9481	0.8437	-0.0871	6.4676	0.0854	: 2003 WP21
4	56.3755	9.3088	25.2534	0.8370	-0.0858	6.3791	0.0902	: 1999 VK12

## Results

## Application

2006NOV11; JD: 2454051.390833



	RA	DEC	Vgeo	U	cos $\beta$	d_RaDec	d_Ucos $\beta$	
	57.8217	14.7193	25.9175	0.8783	-0.1578			: meteor
1	65.8418	20.6078	14.4153	0.7685	-0.0520	9.9497	0.1525	: 2005 UW6
2	59.4412	18.0680	24.7943	0.9398	-0.1795	3.7197	0.0652	: 2010 TU149
3	56.3755	9.3088	25.2534	0.8370	-0.0858	5.6004	0.0831	: 1999 VK12
4	52.9191	15.3793	26.9481	0.8437	-0.0871	4.9467	0.0787	: 2003 WP21

### Conclusions

- We obtained the value of the upper limit of tested D-criteria.
- The threshold value depends on the stream and its orbital evolution.
- We confirm associations with known meteoroid streams for orbits collected in Armagh meteor sample.
- We need to do more analysis and test methods on real data.
- Close encounters clearly prevent us from reconstructing the epoch of origin, even for a slightly perturbed trails.





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