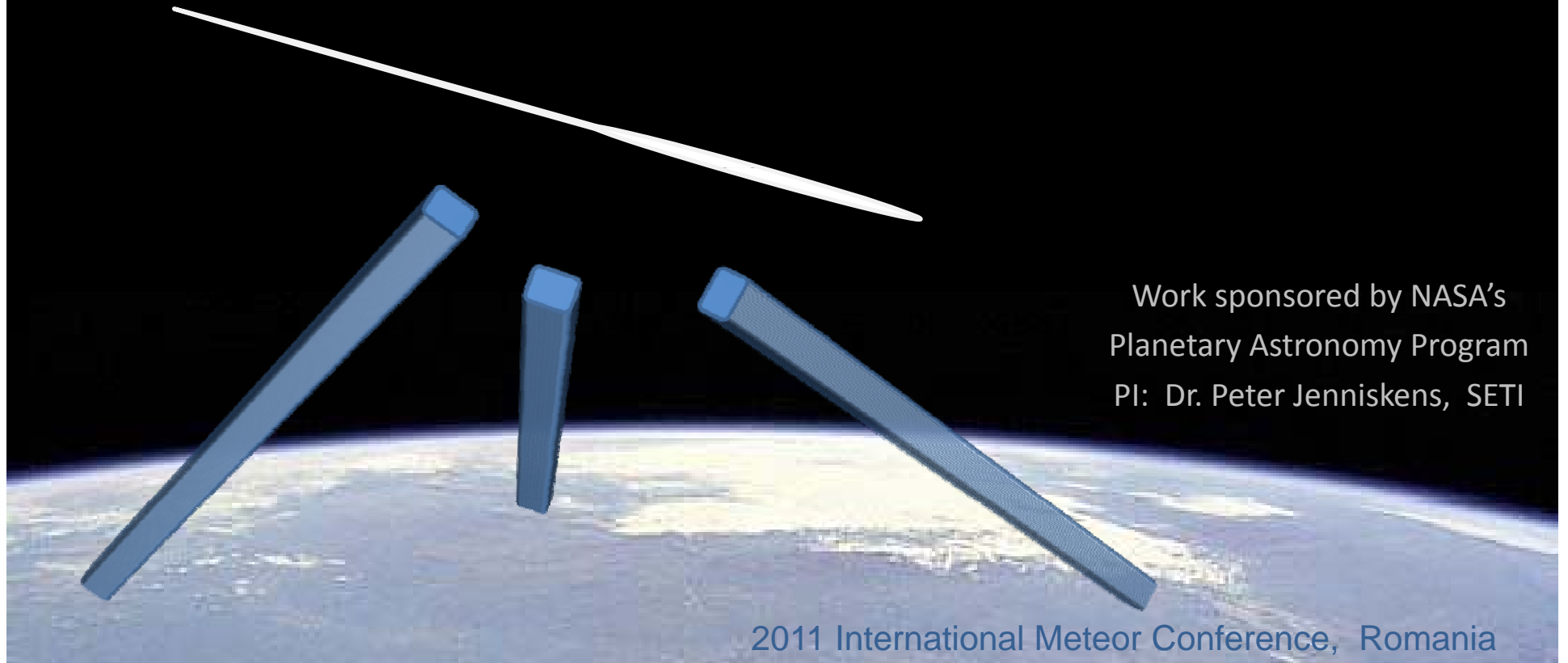


Meteor Trajectory Estimation using Multiple Unsynchronized Video Cameras

Pete Gural

Presented by Damir Segon

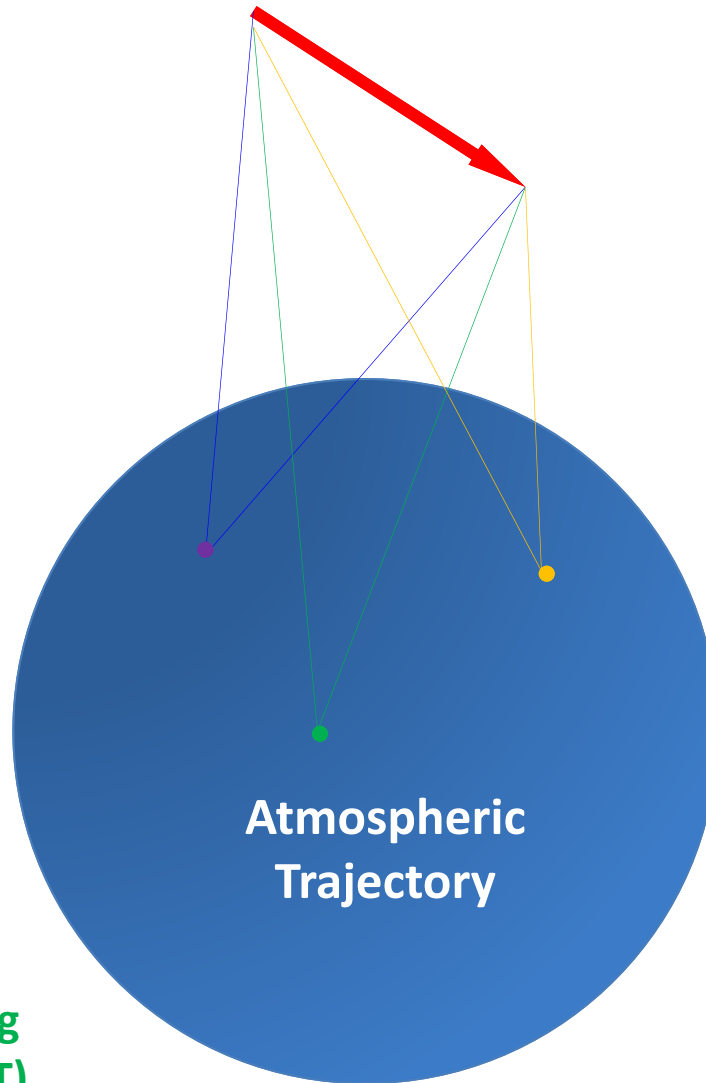
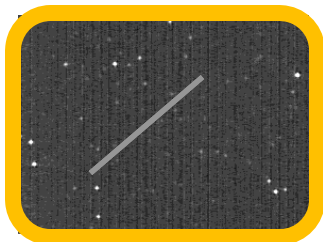
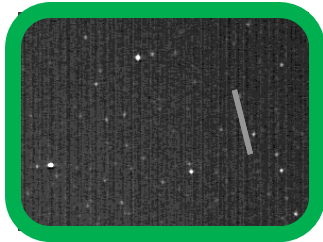
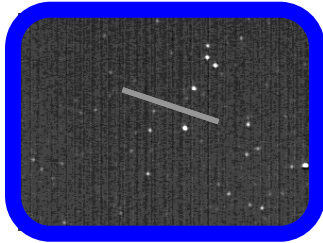


Work sponsored by NASA's
Planetary Astronomy Program
PI: Dr. Peter Jenniskens, SETI

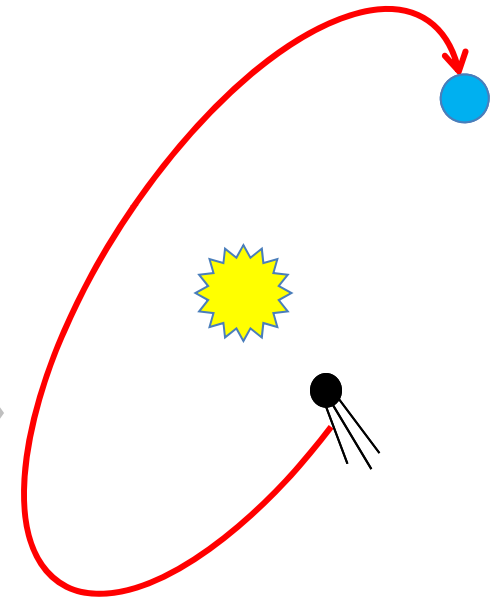
2011 International Meteor Conference, Romania

Problem: Obtain Atmospheric Trajectory via Video Triangulation

Multi-Site Video Measurements



Solar System Orbit



Knowns:

- Camera position/pointing
- Date and approx time (UT)
- FOV astrometry
- Sample rate

Unknowns:

- Radiant direction α, δ
- Meteor position, V_{∞} , deceleration
- Camera timing offsets

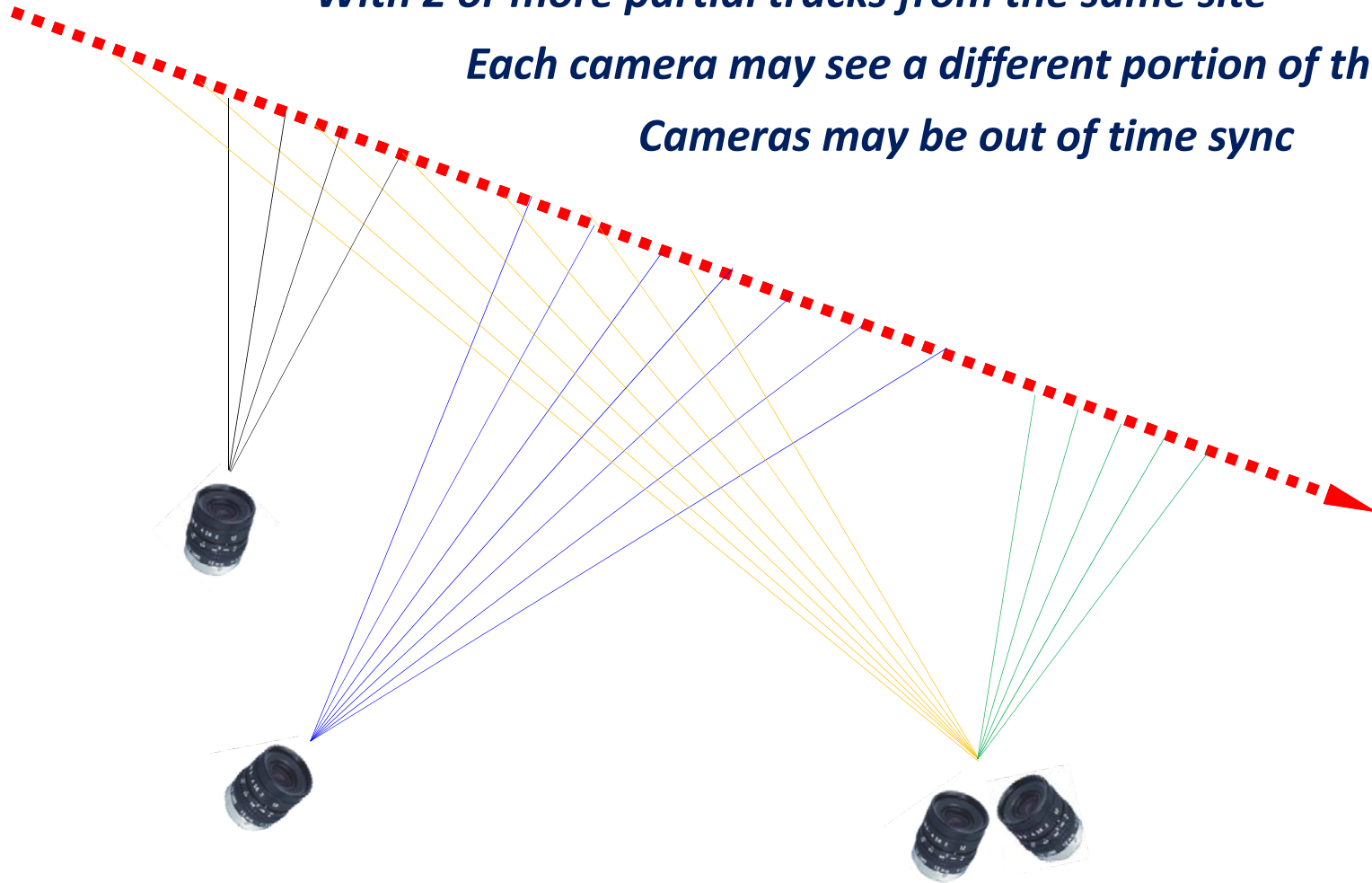
Several deployed systems capture meteors from multiple cameras:

From 2 or more sites

With 2 or more partial tracks from the same site

Each camera may see a different portion of the track

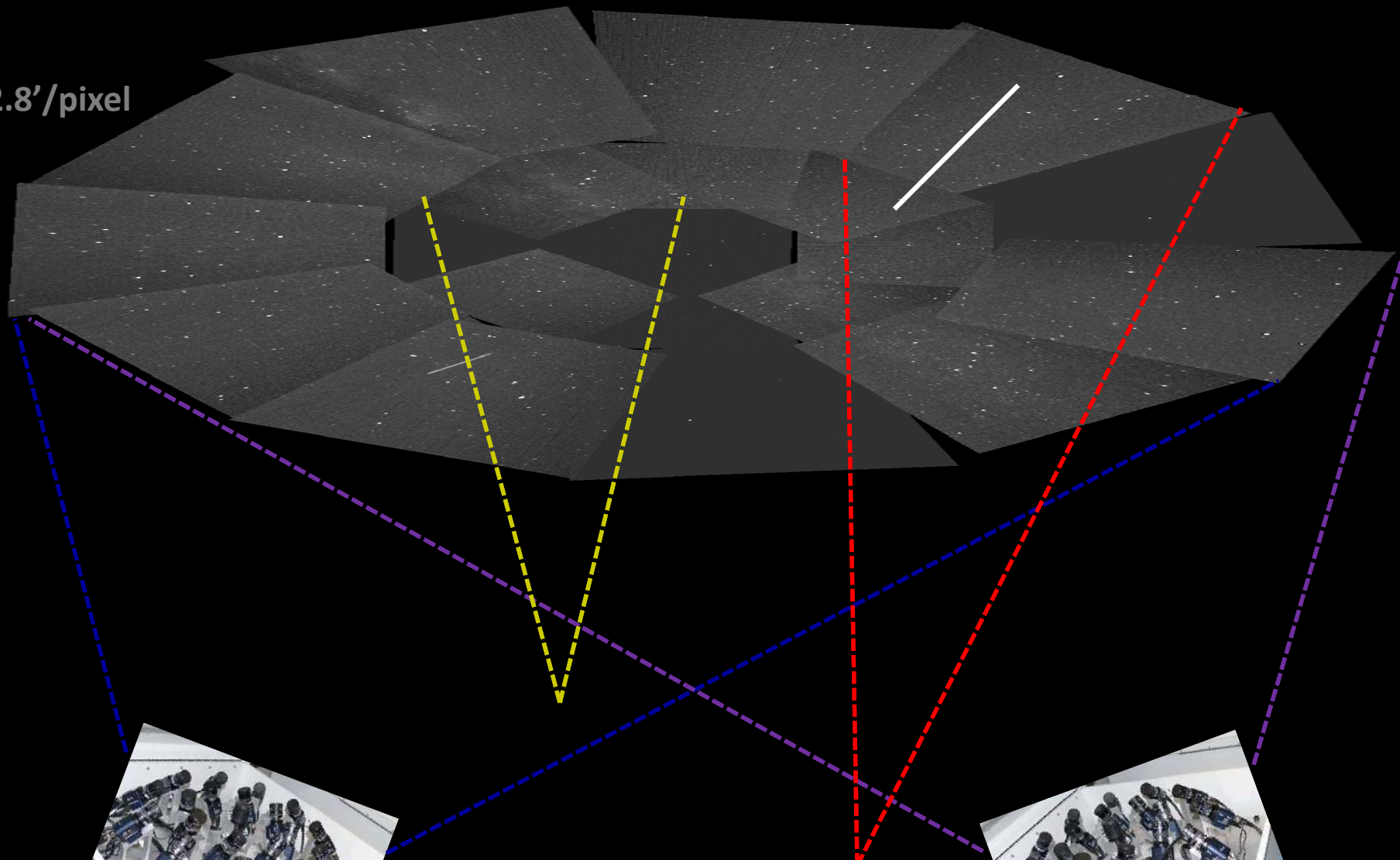
Cameras may be out of time sync



But given space-time coincidence – it is all the same single track !

Example: CAMS All-Sky Coverage from Multiple Video CCDs

2.8'/pixel



Fremont
Peak

+ Bay Area
Amateur Observers

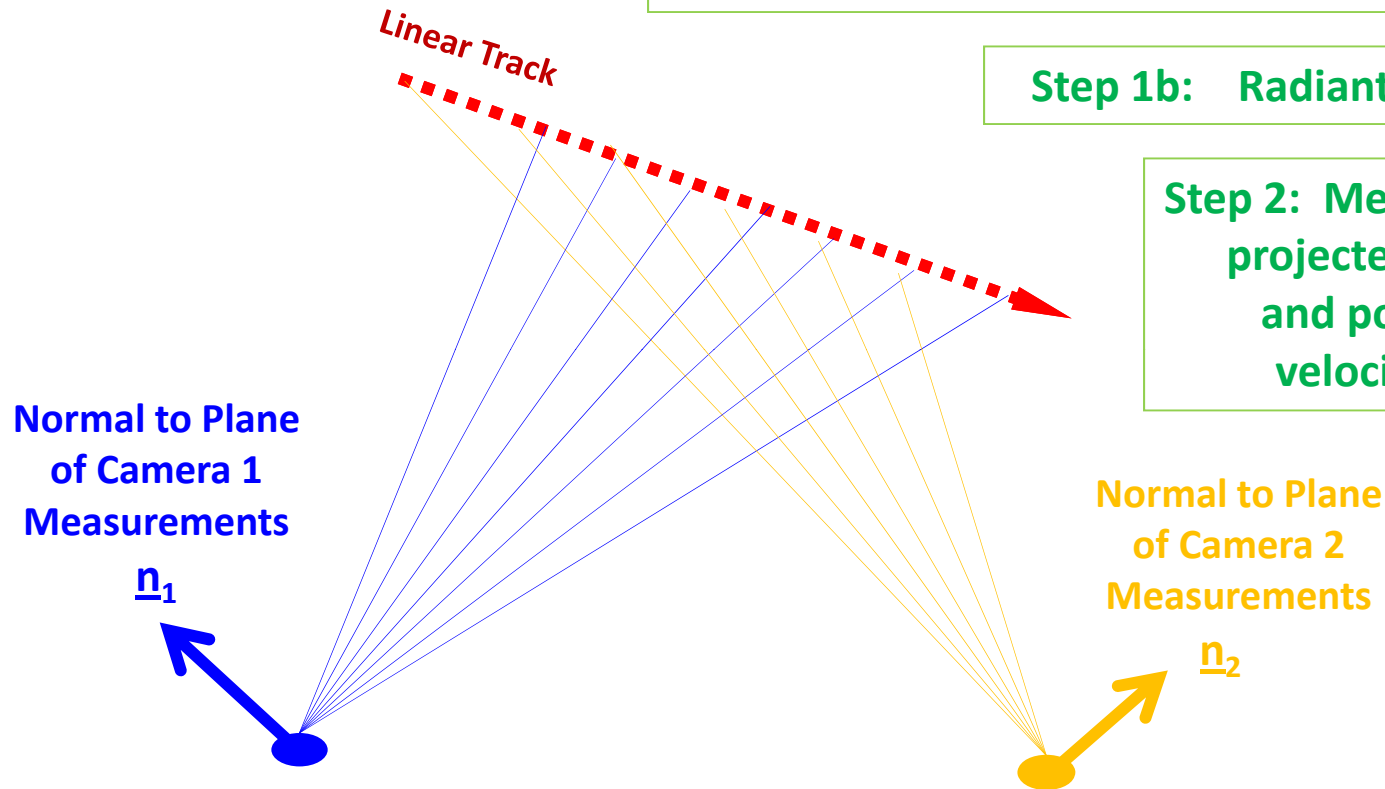
Lick
Observatory

Ceplecha 1987: Intersecting Planes *followed by* LMS fit to Velocity

Step 1a: Find normal to best fitting plane per camera = \underline{n}_k

Step 1b: Radiant Direction = $\underline{n}_1 \times \underline{n}_2$

Step 2: Measurement vectors are projected to CPA of the line and positions are fit for velocity / deceleration

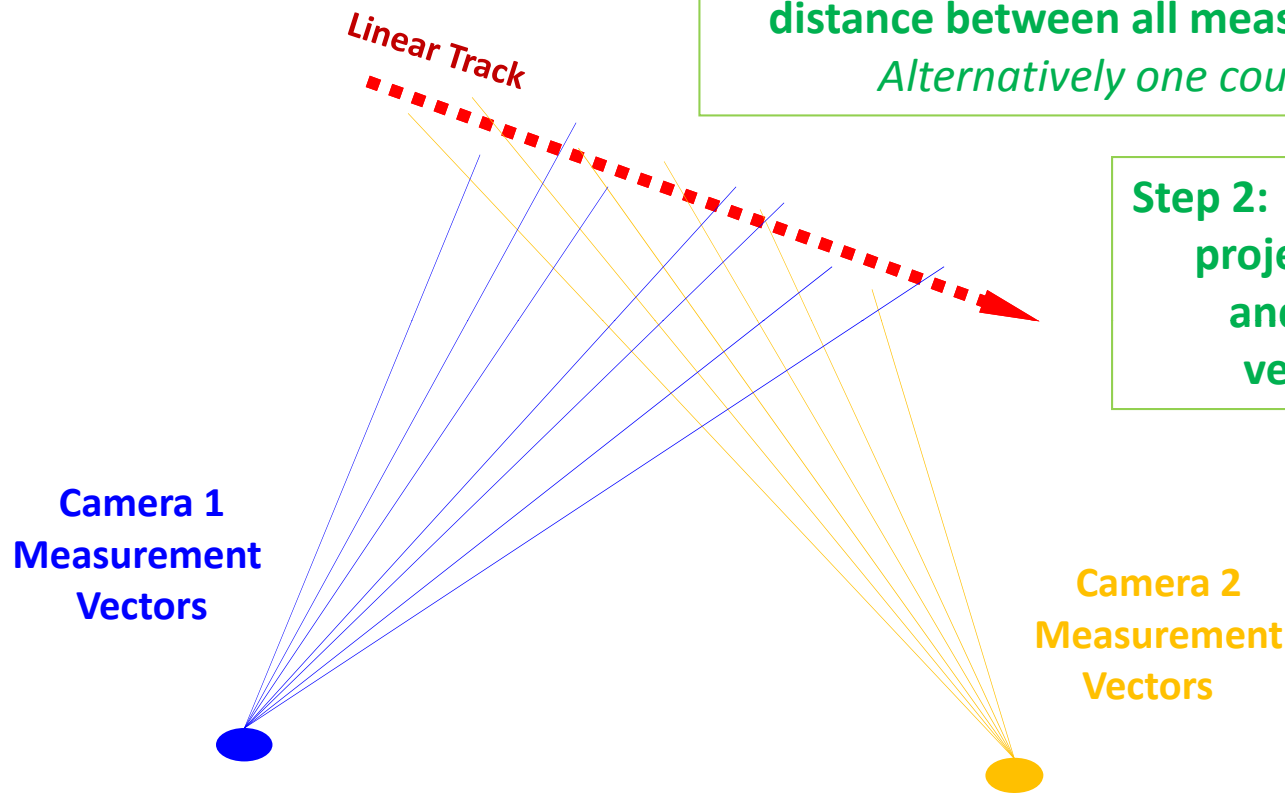


When there are more than two cameras,
several directions are obtained through all possible unique pairings,
and an ad hoc weighting is applied to get a single radiant solution !

Jiri Borovicka 1990: Straight Least Squares Method

Step 1: Solve for a line in 3D space that minimizes the distance between all measurements and that line.
Alternatively one could minimize angle.

Step 2: Measurement vectors are projected to CPA of the line and positions are fit for velocity / deceleration



**This method more naturally handles more than two cameras.
However, it produced equivalent radiant accuracy to intersecting planes !**

New Solution: Fit a Multi-Parameter Motion Model to all Measurements

Single k^{th} Camera Motion Model:

$$\underline{x}_k(t=j\delta_s) = \underline{x}_b + \underline{v}_\infty * [t + \Delta t_k - t_b] + a(t + \Delta t_k - t_b)$$

Number of Unknowns

\underline{x}_b = 3 for position

\underline{v}_∞ = 3 for velocity

a = 0, 1, or 2 for deceleration

Δt_k = #cameras for time offsets

Constrain t to be uniformly spaced δ_s
(NTSC $F_s = 29.97$ Hz)

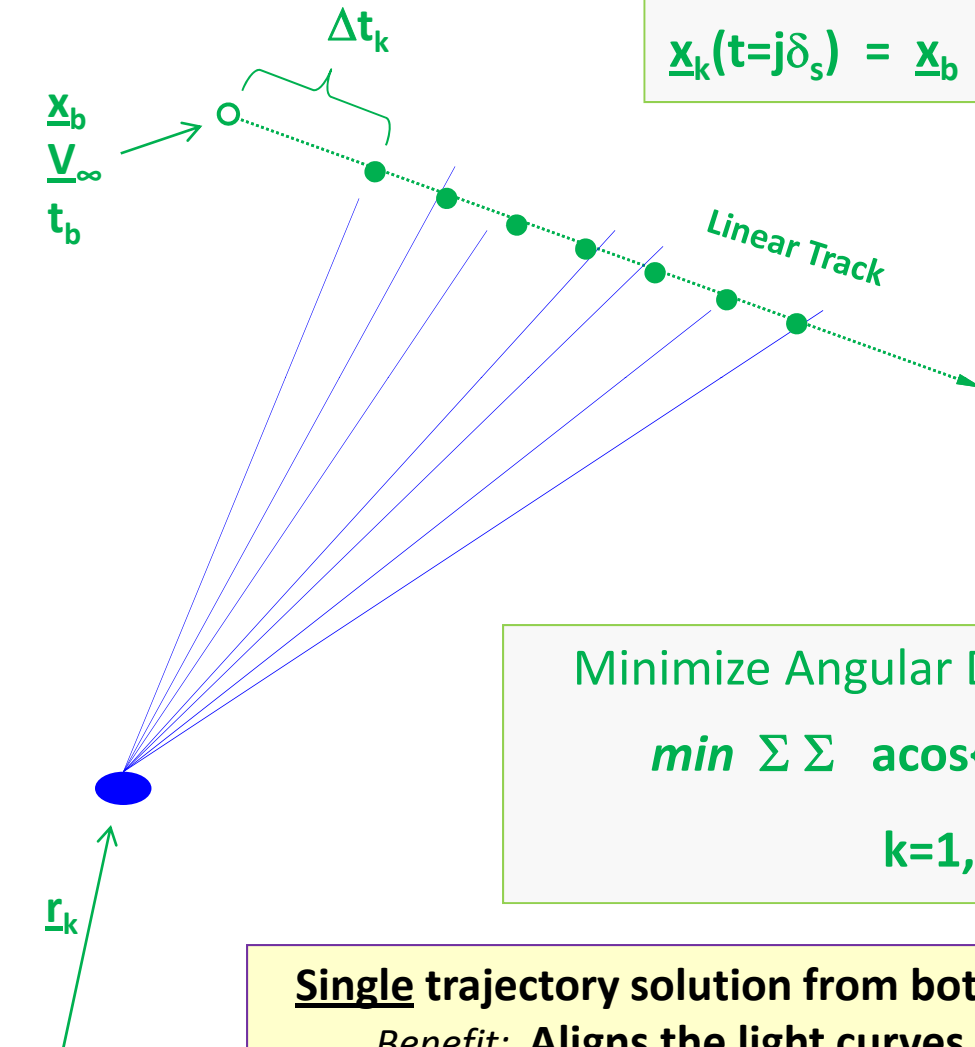
Minimize Angular Distance: Measurement to Model

$$\min \sum_k \sum_j \text{acos}\{ \underline{\text{meas}}(j,k) \cdot [\underline{x}_k(j\delta_s) - \underline{r}_k] \}$$

$$k=1, M_{\text{cams}} \quad j=1, N_{\text{meas}}(k)$$

Single trajectory solution from both same-site and disparate-site cameras !

Benefit: Aligns the light curves even for unsynchronized cameras !

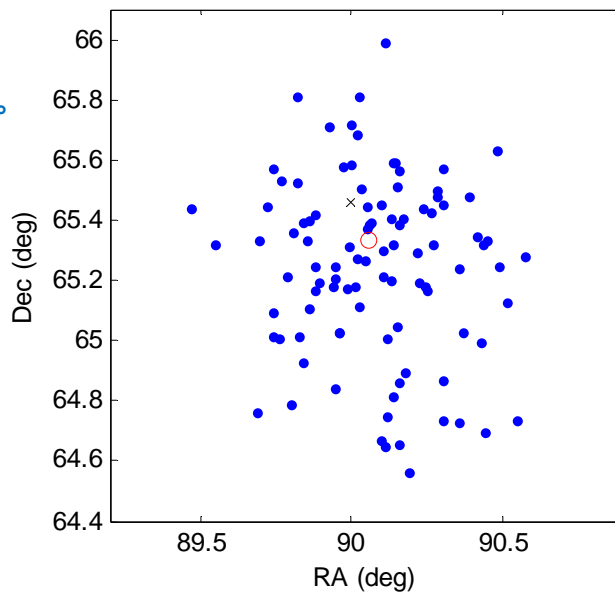


Currently employs a Nelder-Mead, Downhill Simplex, Amoeba minimization

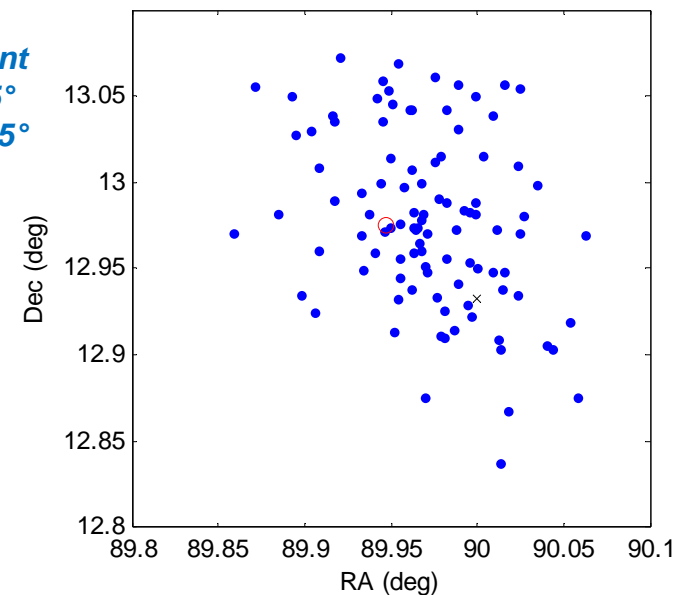
Function Also Provide State Vector Error Estimation

- Error estimates generated for the begin point position and velocity
 - Existing methods try to propagate errors and formulate closed forms expressions
 - New algorithm adds a Monte-Carlo Gaussian distributed error to each measurement
 - Solve over many trials with the baseline solution as the starting parameters
 - Resultant variances are obtained for say 100 trials
 - Feeds into the orbit estimation error analysis

Low Radiant
RA $\sigma = 0.25^\circ$
Dec $\sigma = 0.32^\circ$

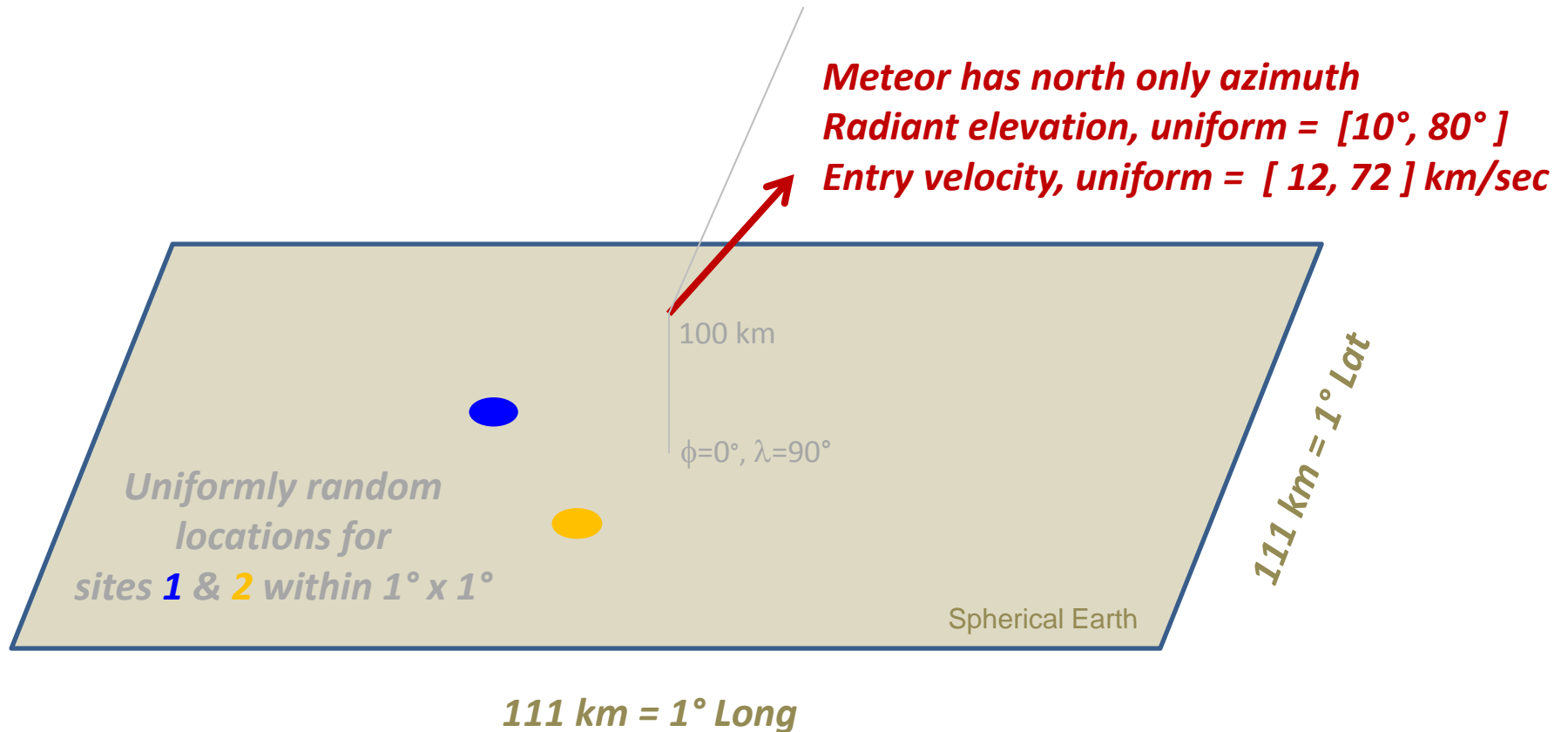


High Radiant
RA $\sigma = 0.05^\circ$
Dec $\sigma = 0.05^\circ$

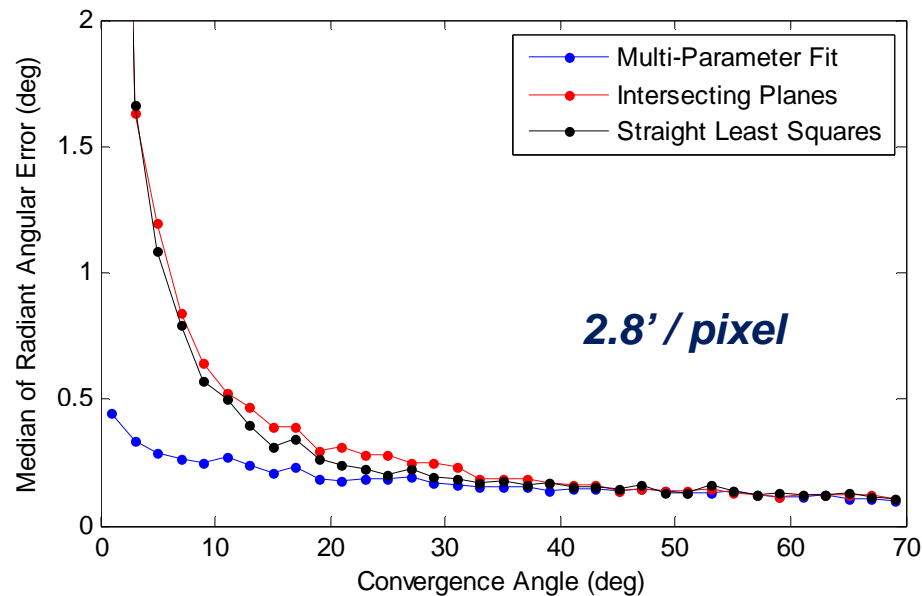
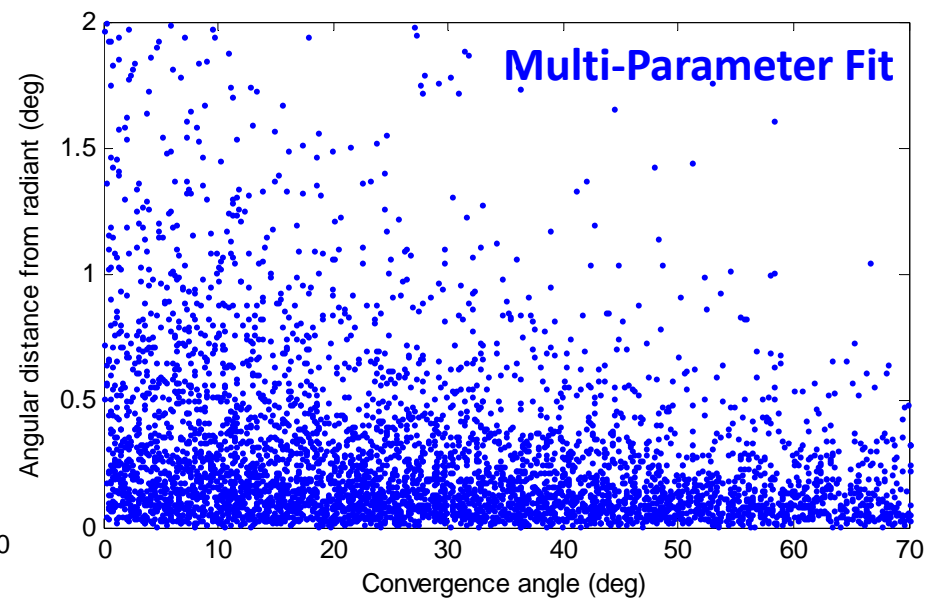
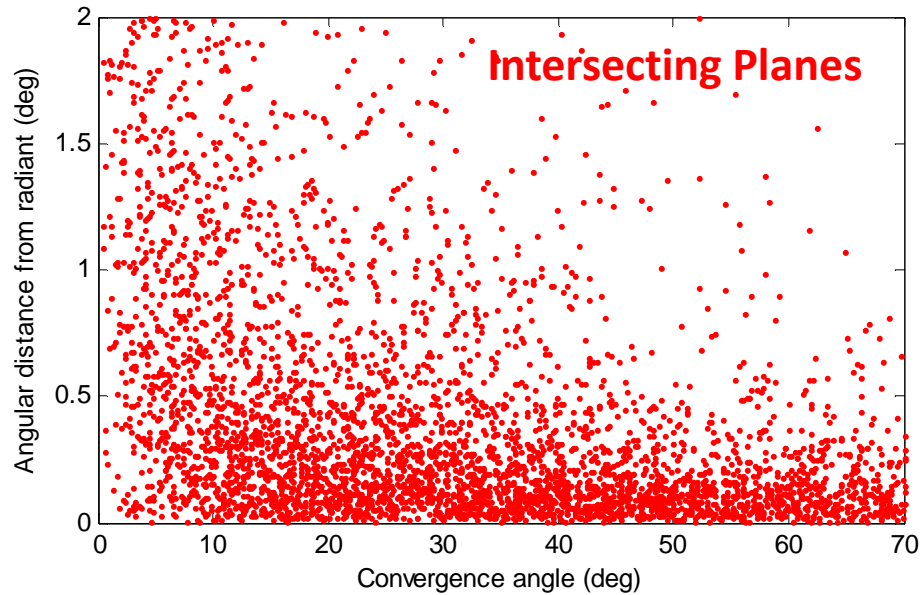


Simulation to Examine Performance

- **Measurement frame rate = 60 Hz** (interleaved row centroids for NTSC)
- **Pixel angular extent = 0.28, 2.8, 10, and 20 arc-minutes**
- **Measurement error Gaussian $\sigma = 0.3$ and 1.0 pixels, 3σ limit**
- **Number of measurements uniformly distributed (integer) = [10, 30]**
- **20,000 Monte-Carlo trials**



Radiant Error versus Convergence Angle

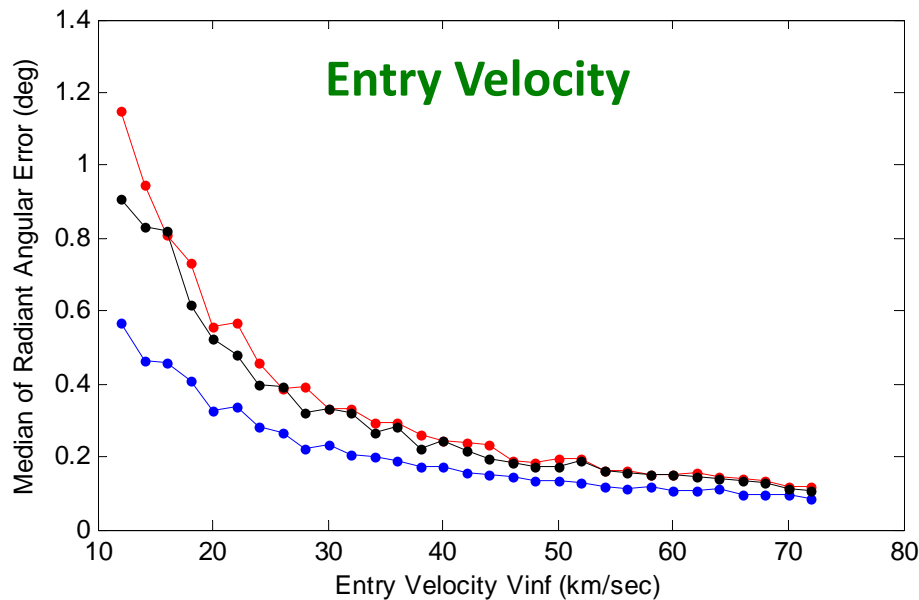
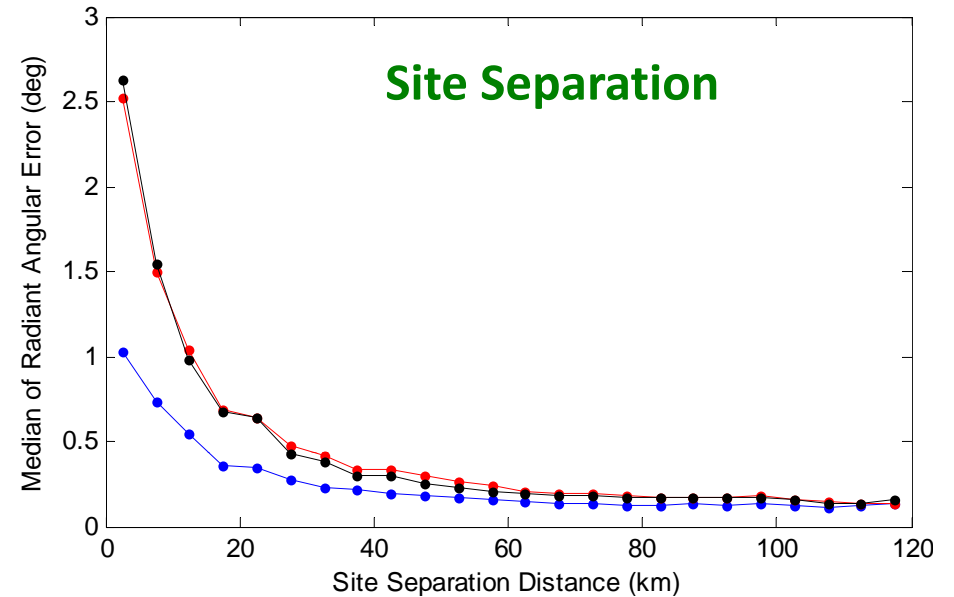
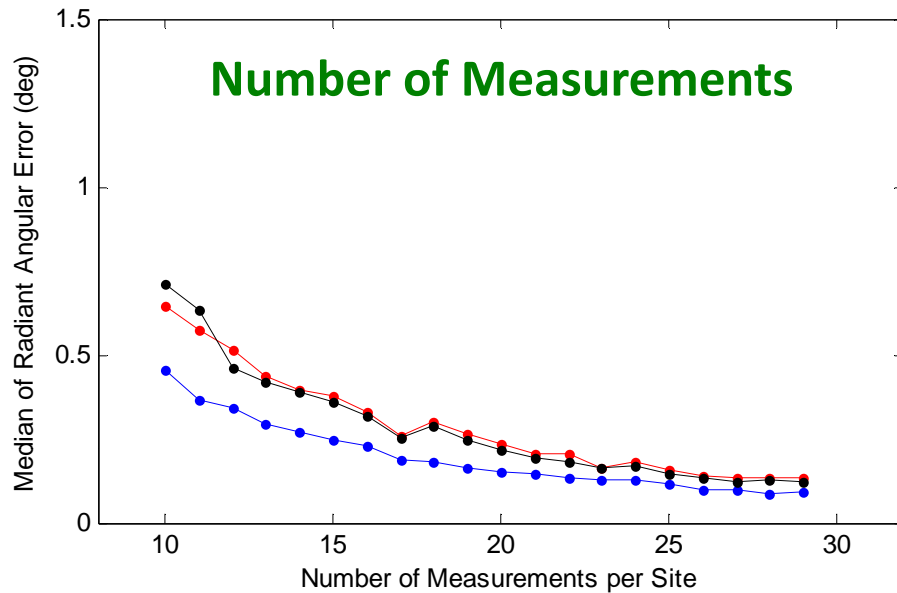


Dr. Jenniskens noticed in CAMS data:

**One can obtain quality solutions
under 30° convergence angle !**

*Explanation: Addition of implicit range
to the angle-angle measurements
arising from the angle subtended
over the video time step.*

Radiant Error Sensitivities to:



It is well known to:

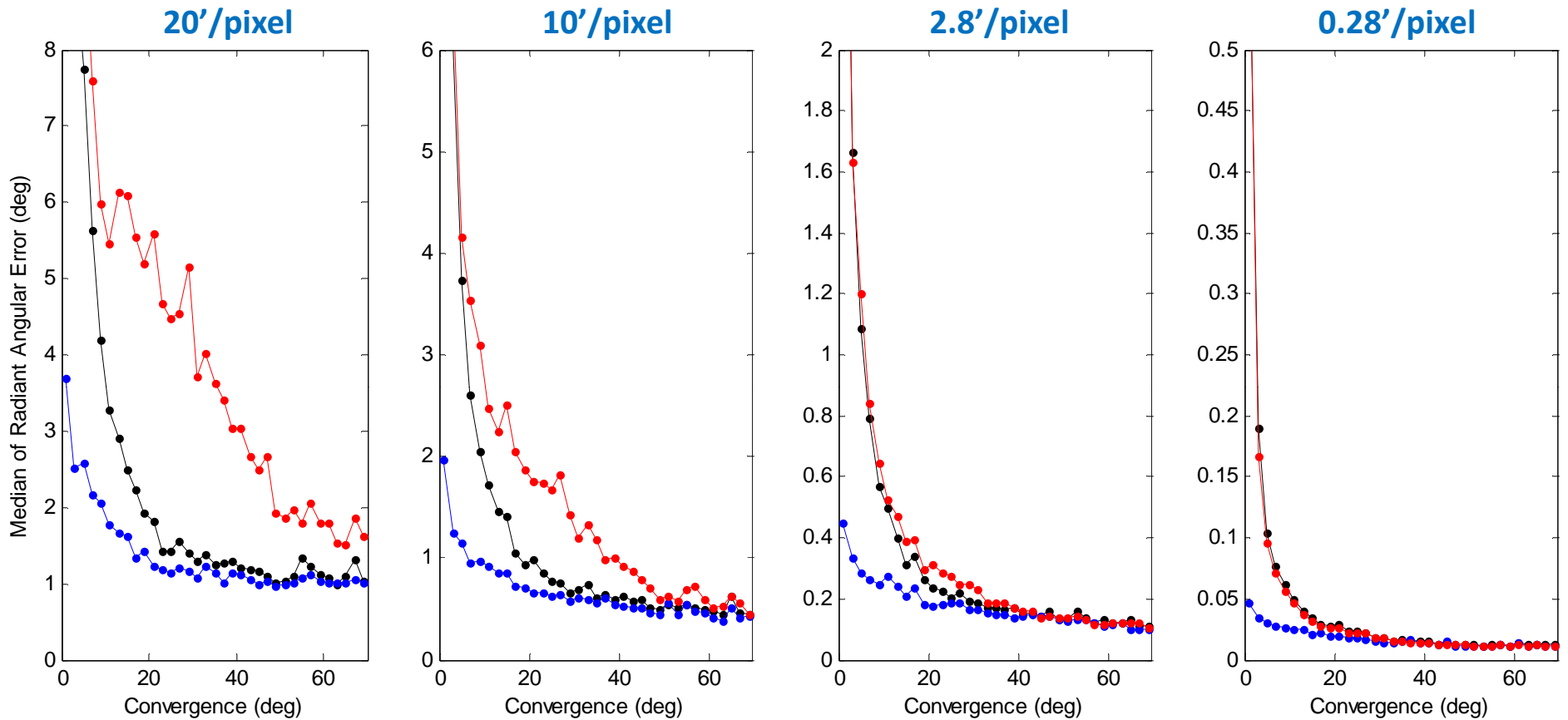
- Separate your observing stations.
- Maximize track length for orientation.

Plots for angular resolution = $2.8'$ /pixel

Meas $\sigma = 0.3$ pixels

60 Hz interleaved row centroid measurements

Radiant Error for Various Sensor Resolutions (Fixed Measurement $\sigma = 0.3$ pixels)

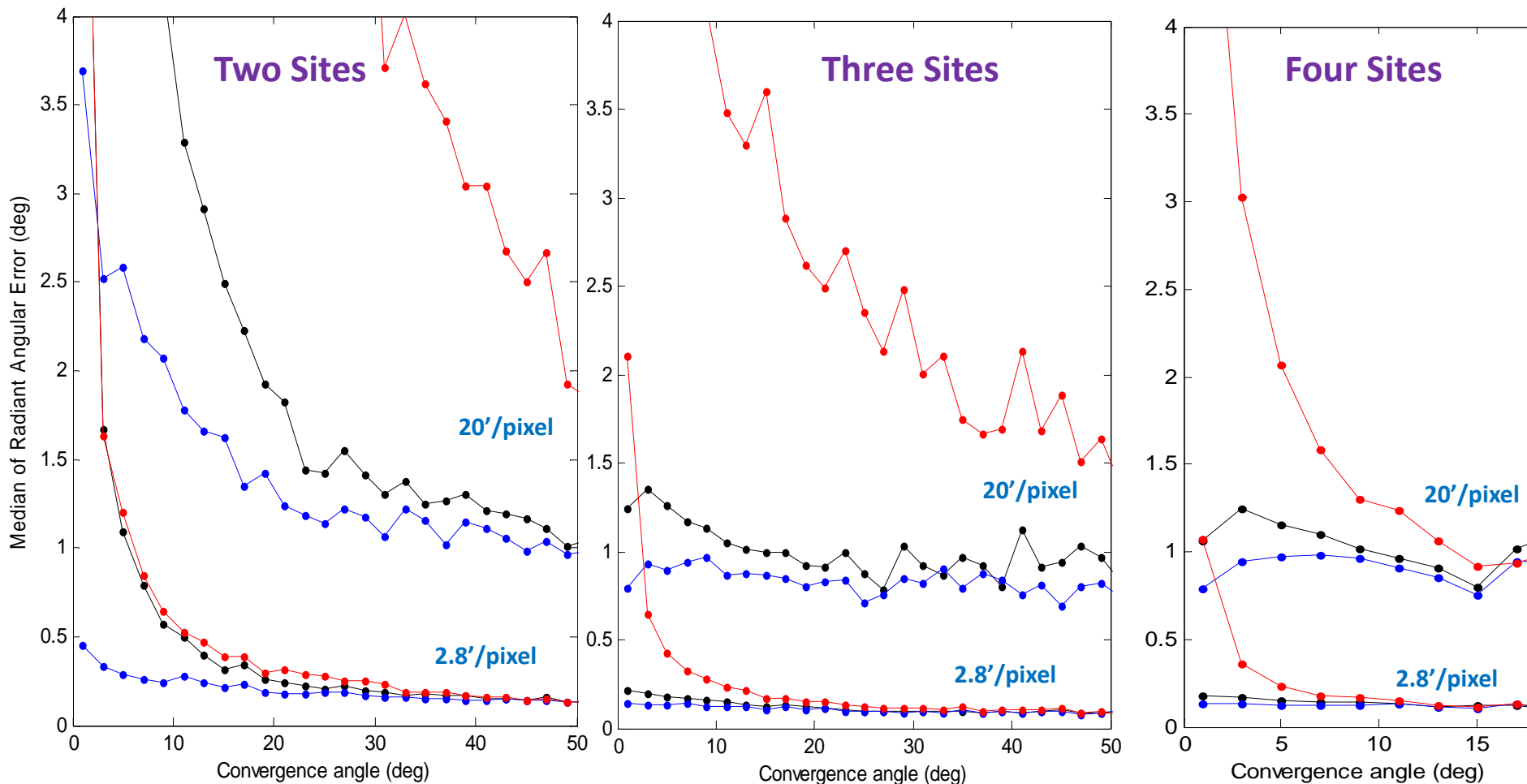


FOV	Sensor Resolution (arcmin / pixel)
160° x 213°	20
80° x 107°	10
22° x 30°	2.8
2.2° x 3°	0.28

Wide field and all-sky cameras can improve their radiant estimation performance !

Note change in vertical scale

Radiant Error Comparing 2, 3, and 4 Observation Sites



Site separation always ≥ 10 km
Measurement error $\sigma = 0.3$ pixels
IP equally weighted average of radiants

With 3 or more sites, the least squares and parameter fit produce equivalent performance !

Summary

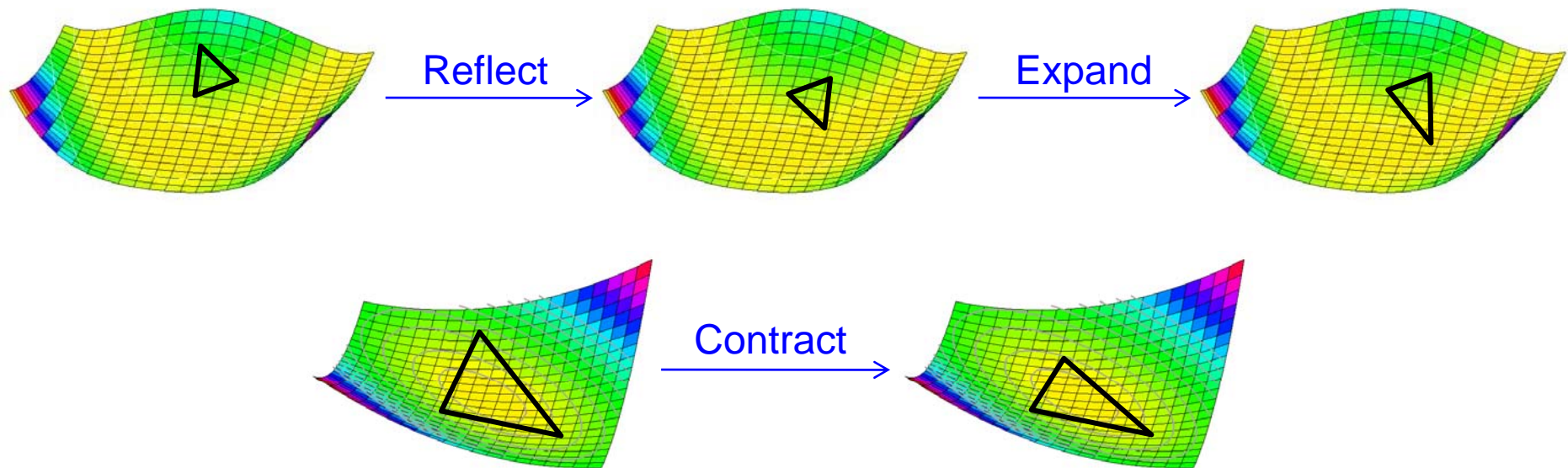
- **New trajectory estimation technique developed**
 - *Multi-parameter fit of multiple un-synchronized cameras to a single-track motion model*
 - *Provides improved accuracy for:*
 - Low convergence angle
 - Smaller site separation
 - *Available as a self-contained C function file “TrajectorySolution.h”*
- **Potential Improvements**
 - *Simulated Annealing minimization*
 - *Add measurement specific error to minimization cost function*
 - *Ingest Azim-N/Elev, Azim-S/ZenAng , versus Ra/Dec only*

Backup Charts

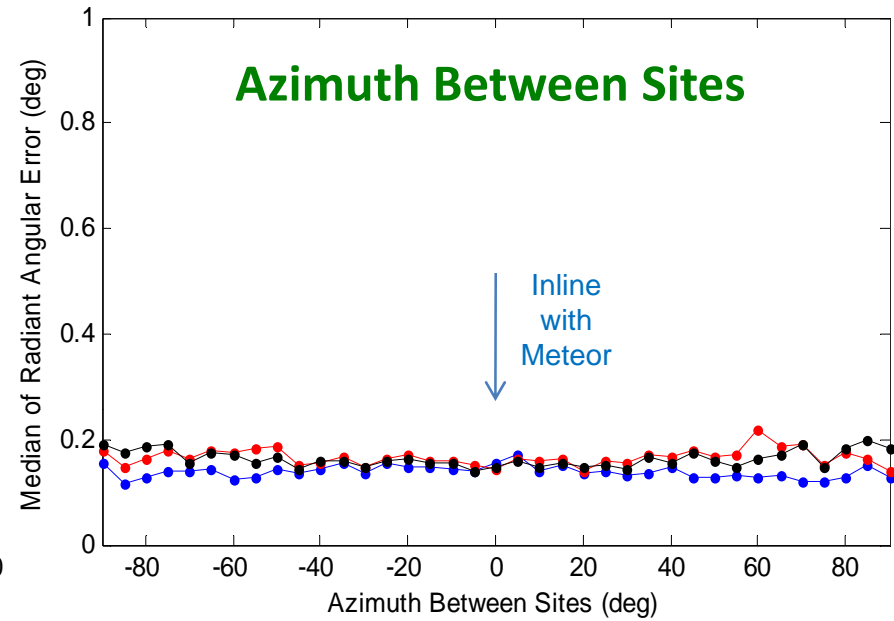
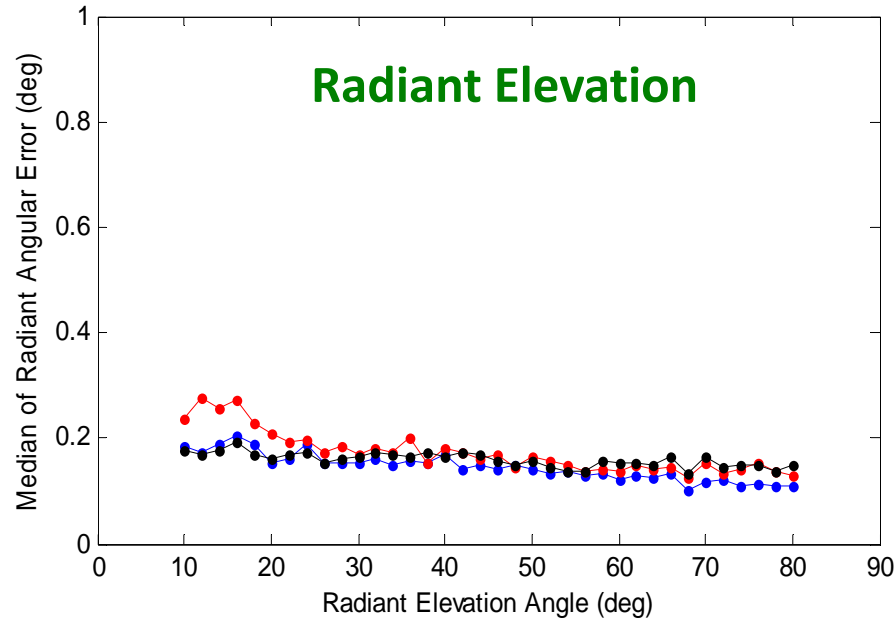
- **Downhill Simplex function minimization**
- **Radiant error insensitivity to meteor geometry**
- **Radiant error for closely separated sites / 5° FOV**
- **Radiant error for various measurement error levels**

Trajectory Minimization Solver Implemented in C

- **Nelder-Mead, Downhill Simplex, or Amoeba minimization**
 - *Function evaluations only, no gradients*
 - *Requires good initial guesses to find global minimum*
 - *Intersecting planes, LMS velocity fit, time offsets solved with others constrained*
 - *Final iterative solution includes all parameters with no constraints*



Radiant Error Insensitive to Meteor Geometry

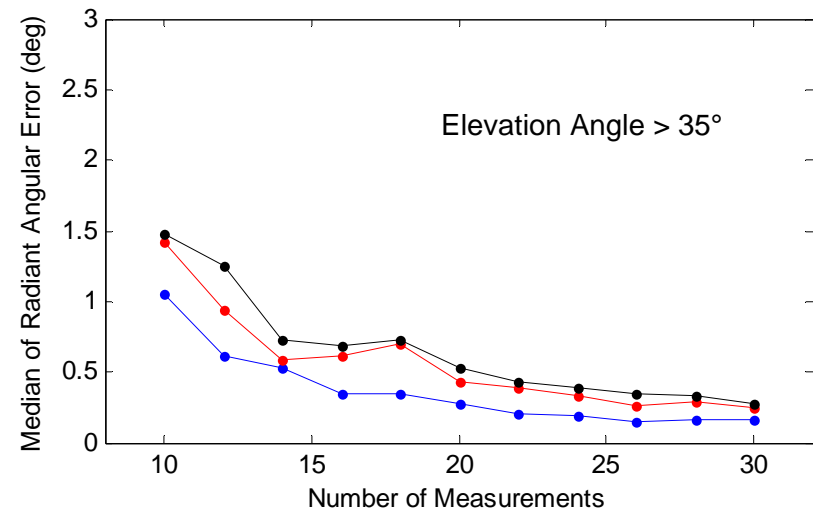
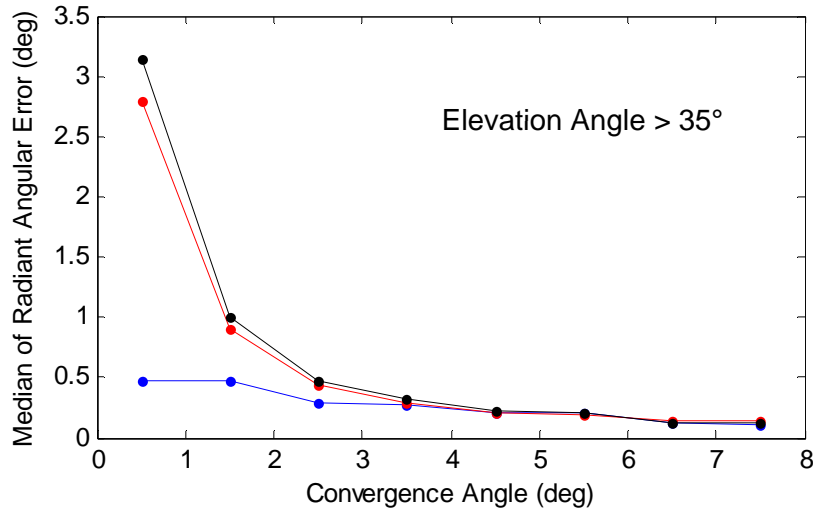
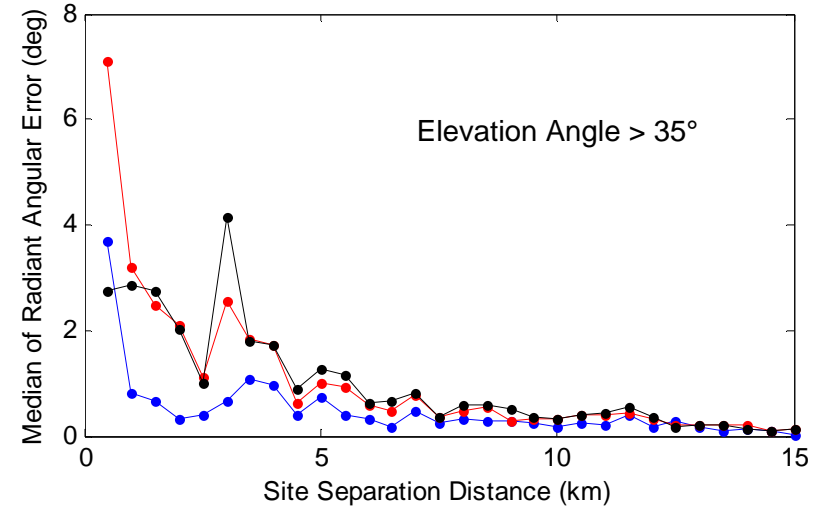
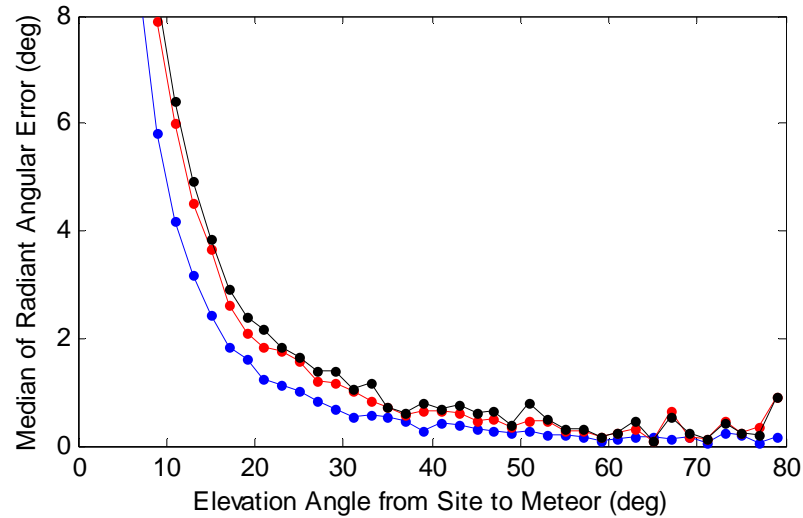


*No obvious dependency on
meteor geometry and site positioning:*

Plots for angular resolution = 2.8'/pixel, meas $\sigma = 0.3$ pixels

Convergence angle > 20°

Radiant Error for Closely Separated Sites / 5° FOV

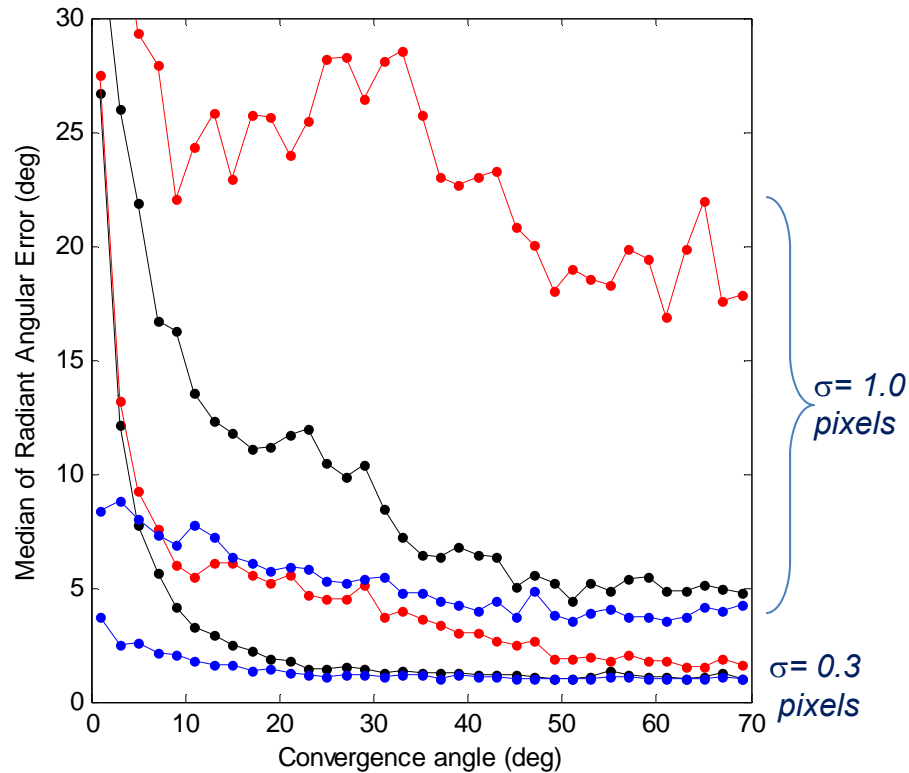


Avoid low elevation angles and hope for long meteors !

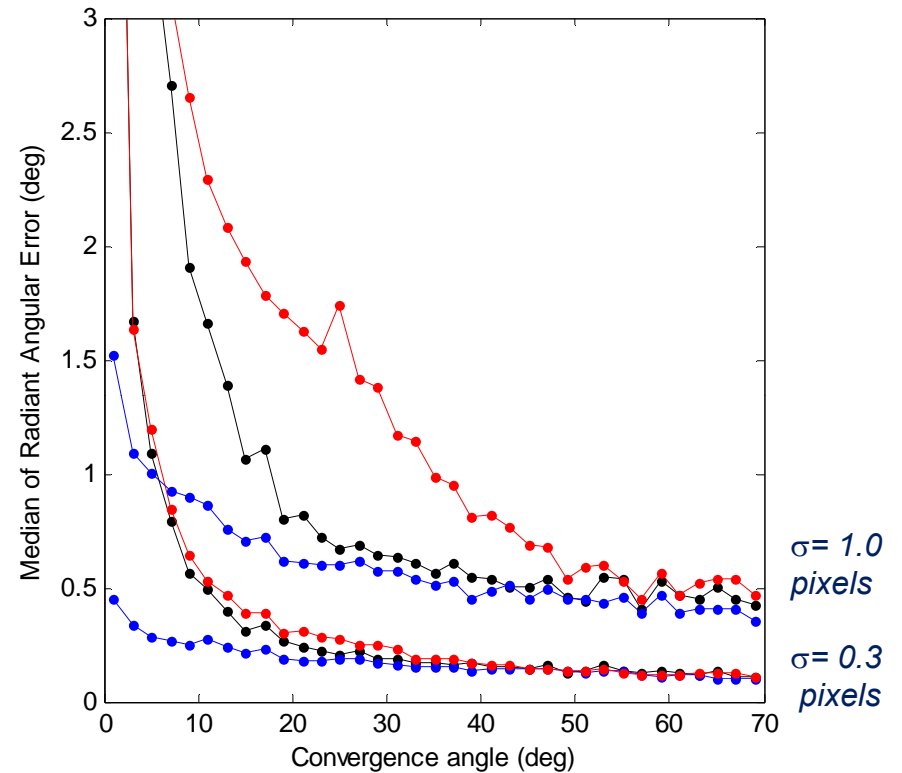
Plots for angular resolution = 0.5'/pixel, meas σ = 0.3 pixels

Radiant Error for Various Measurement Errors (Fixed Sensor Resolution)

Resolution = 20' / pixel



Resolution = 2.8' / pixel



FOV	Sensor Resolution (arcmin / pixel)
160° x 213°	20
80° x 107°	10
22° x 30°	2.8
2.2° x 3°	0.28

Radiant error directly proportional to measurement accuracy for all resolutions (except IP)